

Table of Contents

Preface	ix
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CHAPTER 1. PRELIMINARIES: DISCRETE INDEX SETS AND/OR DISCRETE STATE SPACES

1.1. Non-negative integer valued random variables	1
1.2. Convolution	5
1.3. Generating functions	7
1.3.1. Differentiation of generating functions	9
1.3.2. Generating functions and moments	10
1.3.3. Generating functions and convolution	12
1.3.4. Generating functions, compounding and random sums	15
1.4. The simple branching process	18
1.5. Limit distributions and the continuity theorem	27
1.5.1. The law of rare events	30
1.6. The simple random walk	33
1.7. The distribution of a process*	40
1.8. Stopping times*	44
1.8.1. Wald's identity	47
1.8.2. Splitting an iid sequence at a stopping time *	48
Exercises for Chapter 1.	51

CHAPTER 2. MARKOV CHAINS

2.1. Construction and first properties	61
2.2. Examples	66
2.3. Higher order transition probabilities	72
2.4. Decomposition of the state space	77
2.5. The dissection principle	81
2.6. Transience and recurrence	85
2.7. Periodicity	91
2.8. Solidarity properties	92
2.9. Examples	94
2.10. Canonical decomposition	98
2.11. Absorption probabilities	102
2.12. Invariant measures and stationary distributions	116

*This section contains advanced material which may be skipped on first reading by beginning readers.